



Analytical Survey on the Two-Fluid Blood Flow through Stenosed Artery with Permeable Wall

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Abstract

The womersley flow of blood through constricted arteries is analyzed by considering the blood as a two-fluid model with the suspension of all the erythrocytes within the core region as a non-Newtonian fluid and also the plasma within the peripheral layer as a Newtonian fluid. The non-Newtonian fluid within the core region of the artery is assumed as a Herschel-Bulkley fluid and Casson fluid. The perturbation technique is employed to resolve the ensuing system of non-linear partial differential equations. Expressions for numerous flow quantities are obtained for the two-fluid Casson model. In the present paper, there's associate analysis on the varied researches. It's determined that the plug core radius, pressure drop, wall shear stress and also the resistance to flow are considerably terribly low for the two-fluid Casson model than those of the two-fluid Herschel-Bulkley model. Hence, the two-fluid Casson model would be a lot of helpful than the two-fluid Herschel-Bulkley model to research the blood flow through constricted arteries.

Keywords: Artery, Blood, Mathematical modeling, Permeable wall.

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